CALCULUS - Curve Sketching Worksheet

For each function, perform the first and second derivative test, then graph the function.

1)
$$y = -\frac{x^3}{3} + x^2$$

2)
$$y = -\frac{x^4}{4} + x^2 - 1$$

Use the given information to graph the function. 3.

x-intercepts at
$$x = -6, 4$$

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y-intercept at $y = \frac{12\sqrt[3]{2}}{5}$

Critical points at: x = 0, 4

Increasing: $(-\infty, 0)$, $(4, \infty)$

Decreasing: (0, 4)

Inflection point at: x = 6

Concave up: (6, ∞)

Concave down: $(-\infty, 4)$, (4, 6)

Relative minimum: (4, 0)

Relative maximum:
$$\left(0, \frac{12\sqrt[3]{2}}{5}\right)$$